Algorithms and Framework for Energy Efficient Parallel Stream Computing on Many-Core Architectures

#### **Nicolas Melot**



Linköping University Dept. of Computer and Inf. Science Linköping, Sweden

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## Outline

#### 1 Introduction

2 Crown Scheduling

#### 3 Drake

#### 4 Conclusion



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Introduction		Conclusion
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Constant struggle for performance





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Introduction		
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Constant struggle for performance: Hollerith census machine

Census every 10 years.



Picture: "HollerithMachine.CHM" by Adam Schuster

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Introduction		
● <b>○</b> ○		

Constant struggle for performance: Hollerith census machine

- Census every 10 years.
- 8 years in 1880.



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Introduction		
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Constant struggle for performance: Hollerith census machine

- Census every 10 years.
- 8 years in 1880.
- 1 year in 1890.



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Drai

Conclusion

# High performance computing

Constant struggle for performance: Big data.

- Social medias
- Internet of things





Introduction		
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Constant struggle for performance: Big data.

Social medias

Internet of things

Applications:

Scientific computing

Picture: "View inside detector at the CMS cavern LHC CERN" by Tighef

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Introduction		
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Constant struggle for performance: Big data.

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- Internet of things
- Applications:
  - Scientific computing
  - Marketing

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Introduction		
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Introduction		
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Applications:

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- Marketing
- Intelligence (GCHQ)

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Introduction		
Accelerate co	omputation	



Introduction ○○●		
Accelerate o	computation	

How to improve performance?

Miniaturize

End of Moore's law?



Introduction		Conclusion

- Miniaturize
  - End of Moore's law?
- Increase frequency
  - Too high energy consumption





Introduction		Conclusion

- Miniaturize
  - End of Moore's law?
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  - Too high energy consumption
- Parallel programming





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Introduction		Conclusion

- Miniaturize
  - End of Moore's law?
- Increase frequency
  - Too high energy consumption
- Parallel programming
  - Better energy consumption
  - Very challenging
    - Instruction-Level parallelism
      Wall





Introduction ○○●		Conclusion

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    - Scalability issues for consistent shared memory





Introduction ○○●		Conclusion

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  - Better energy consumption
  - Very challenging
    - Instruction-Level parallelism
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    - Scalability issues for consistent shared memory
    - Von-Neumann bottleneck





Crown Scheduling	

## Streaming computation

#### Streaming

- Software pipelining
- Tasks execute in parallel in steady-state



Figure: Streaming taskgraph.



Figure: Pipelined execution of streaming taskgraph.



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# Streaming computation

#### Streaming

- Software pipelining
- Tasks execute in parallel in steady-state

## Static scheduling

- Moldable tasks
- Steady state
- Throughput constraint
- Optimize energy



#### Figure: Streaming taskgraph.



# Figure: Steady state of the streaming pipeline.



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# Streaming computation

#### Streaming

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## Static scheduling

- Moldable tasks
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- Throughput constraint
- Optimize energy

Streaming Task Collection

- Independent tasks
- Balance workload
  - No communication cost



Figure: Streaming taskgraph.



Figure: Independent tasks in the steady state.

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## Platform model

#### Platform

- p uniform processors
- Discrete frequency set F
  - Applied to individual cores
  - Voltage by auto-co-scaling
  - Can change dynamically any time

Power model

- Dynamic power function of frequency
  - Analytic function or measurements
  - No restriction
  - Replaceable

Energy linear in time, power and number of processors running



Introduction 000	Crown Scheduling	
Task model		

#### Moldable task j

- Fixed work τ<sub>j</sub>
- Allocation: run on  $w_j \ge 1$  cores
  - Maximum  $W_j$ :  $w_j \leq W_j$
- Arbitrary efficiency function
  - $0 < \mathbf{e}_j(\mathbf{q}) \le 1$  for  $1 \le \mathbf{q} \le \mathbf{W}_j$
  - No convexity, monotony or continuity constraint
- Time proportional to work, parallel degree and frequency



Figure: Arbitrary efficiency function.



Figure: Moldable task.



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# Problem formulation

- 3 static problems
  - Resource allocation
    - Find  $w_j \leq min(p, W_j)$  for each task j
    - Define execution time of tasks j
  - Task mapping to cores
    - Assign tasks to a subset of cores 1..p
  - Discrete frequency scaling
    - Assign tasks a frequency level in F
    - Respect a makespan constraint M
  - Repeated execution of a task sequence
  - Non data-ready tasks are delayed to the next round





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## All steps influence each other





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## Restrict allocation and mapping to O(p) processor subsets (groups)





- Tasks must be allocated as many cores as the size of a group
- Reduce possible mapping targets from  $2^p 1$  groups to 2p 1

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Crown schee	duling	

#### Computing a crown schedule

Separated or integrated phases



- ILP formulations for each step and for integrated scheduler by (Kessler et al. [2013])
  - Phase separation prevents compromises
  - Phase integrated constrained by the crown structure
  - Slow and limited in input problem size



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Crown Scheduling	

# **Crown Extensions**

#### Adapt to realistic processors

- $\square p \neq 2^i$
- Constraints: frequency islands





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## **Crown Extensions**

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## **Crown Configuration**





Crown Scheduling	

## **Crown Extensions**

#### Adapt to realistic processors

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**Crown Configuration** 

#### **Crown Consolidation**

- Account for idle energy
- Switch unused cores off




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## **Crown Extensions**

#### Adapt to realistic processors

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**Crown Configuration** 

#### **Crown Consolidation**

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### Provable approximation







# Voltage Islands topology influence







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# Voltage Islands topology influence









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## Voltage Islands topology influence







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## Developed by JohN Von Neumann in 1945 (Knuth [1998])

External algorithm



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Developed by JohN Von Neumann in 1945 (Knuth [1998])

- External algorithm
- Limits use of slow memories





Streaming over Manycores

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- *External* algorithm
- Limits use of slow memories
- Stream program: tree structure





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  - other: merge (streamed)





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  - Root task: biggest workload





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  - Leaves: presort (non-streamed)
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  - Root task: biggest workload
  - 2<sup>nd</sup> level tasks: half workload of root task





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https://www.youtube.com/watch?v=XaqR3G\_NVoo



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#### All cores in one island: 100%







Crown Scheduling	
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## All cores in one island: 100%



#### Individual cores: 30%







Crown Scheduling	
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Crown Scheduling	
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#### 2 islands of 16 cores: 47%



#### Individual cores: 30%



Legend





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Streaming over Manycores

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Legend



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Streaming over Manycores





	Drake ●O	Conclusion
Drake		

### Stream programming framework

On-chip pipelining



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	Drake	

### Stream programming framework

- On-chip pipelining
- Moldable tasks



	Drake ●○	Conclusion
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### Stream programming framework

- On-chip pipelining
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- Scheduling experiments (Melot et al. [2015])



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	Drake	

## Stream programming framework

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## Drake: derived from Schedeval (Janzén [2014])

### Separate roles in an application



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Streaming over Manycores

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	Drake	

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Separate roles in an application

## Stream topology



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	Drake	

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Separate roles in an application

- Stream topology
- Tasks' source code



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	Drake	

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Target platform-specifics

Diala		
	00	Conclusion
	Drake	Conclusion

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Separate roles in an application

- Stream topology
- Tasks' source code

- Target platform-specifics
- Host application

Streaming over Manycores

		Drake ⊙●	
Drake C Stream	ning Framework		

Takes code to execute on target platform

Application-specific: Mergesort, FFT, etc.



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- Application-specific: Mergesort, FFT, etc.
- Platform-specific: SCC, Xeon, MPI, etc.
  - Message passing


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		Conclusion
Conclusion		

# Challenges in high-performance parallel computing

Programming difficulties



Constant stars		
		Conclusion

Challenges in high-performance parallel computing

- Programming difficulties
- Lack of scalability of architectures



	Conclusion

Challenges in high-performance parallel computing

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- Von Neumann bottleneck



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Stream programming

Mature research



	Conclusion

Challenges in high-performance parallel computing

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- Mature research
- No need of coherent shared memory



		Conclusion
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Challenges in high-performance parallel computing

- Programming difficulties
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- Help reduce von Neumann bottleneck



		Conclusion
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Challenges in high-performance parallel computing

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Our contributions

On-chip pipelining

- Mature research
- No need of coherent shared memory
- Help reduce von Neumann bottleneck



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# Our contributions

- On-chip pipelining
- Crown Scheduling for Moldable Streaming tasks

- Mature research
- No need of coherent shared memory
- Help reduce von Neumann bottleneck



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#### Our contributions

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- Crown Scheduling for Moldable Streaming tasks
- Drake Streaming Framework



		Conclusion

Investigate more scheduling techniques

 Minimize communication costs



	Conclusion

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- Heterogeneous platforms



	Conclusion

- Minimize communication costs
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- Quasi-static scheduling



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- Schedule main memory accesses



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- Implement Synchronous Data
  Flow for Drake



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# Simultaneous Localization And Mapping



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### Simultaneous Localization And Mapping



Other applications:

Machine learning

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# Simultaneous Localization And Mapping



Other applications:

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#### Simultaneous Localization And Mapping



Other applications:

- Machine learning
- Provable High Performance Computing
- Aeronautic

		Conclusion
Questions		

Thank you for your attention.



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